

STAT 3202: Practice 04

Autumn 2018, OSU

Exercise 1

Consider a random sample X_1, X_2, \dots, X_n from a normal distribution with mean μ and variance σ^2 .

(a) Calculate a 95% confidence interval if

- $n = 6$
- $\bar{x} = 21.4$
- $s^2 = 0.64$

(b) Calculate a 99% confidence interval if

- $n = 12$
- $\bar{x} = 5.7$
- $s^2 = 9$

(c) Calculate a 90% confidence interval if

- $n = 15$
- $\bar{x} = 42.1$
- $s = 11$

(d) Calculate a 90% confidence interval if

- $n = 42$
 - $\bar{x} = 17.2$
 - $s = 8$
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Exercise 2

Suppose that the amount of cereal dispensed into a box is normally distributed. If the mean amount dispensed in a box is “too small,” then the proportion of “underfilled” boxes (boxes with less than 16 ounces of cereal in them) is too large. However, if the mean is “too large,” then the company loses money “overfilling” the boxes. The CEO of the company that makes *Captain Crisp* cereal, Mr. Statman, is concerned that the machines that dispense cereal into boxes do not have the proper (“optimal”) setting for the mean amount dispensed. A random sample of 196 boxes was obtained, the sample mean amount of cereal in these 196 boxes was 16.07 ounces, the sample standard deviation was 0.21 ounces.

Construct a 95% confidence interval for the current mean amount of cereal dispensed into a box.

Exercise 3

In a random sample of 25 direct flights from New York to Boston by *Hawk & Hummingbird Airline*, the sample mean flight time was 56 minutes and the sample standard deviation was 8 minutes. (Assume the

flight times are approximately normally distributed.)

Construct a 99% confidence interval for the overall mean flight time on this route.

Exercise 4

Consider the following random sample which was obtained from a normal distribution with some unknown mean μ and unknown variance σ^2 :

$$x_1 = 16, x_2 = 12, x_3 = 18, x_4 = 13, x_5 = 21, x_6 = 15, x_7 = 8, x_8 = 17$$

- (a) Construct a 95% confidence interval for μ .
 - (b) Construct a 90% confidence interval for μ .
 - (c) Construct a 99% confidence lower bound for μ .
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Exercise 5

Just prior to an important election, in a random sample of 749 voters, 397 preferred Candidate Y over Candidate Z. Construct a 90% confidence interval for the overall proportion of voters who prefer Candidate Y over Candidate Z.

Exercise 6

An article on secretaries' salaries in the Wall Street Journal reports: "Three-fourth of surveyed secretaries said they make less than \$25,000 a year." Suppose that the Journal based its results on a random sample of 460 secretaries drawn from every category of business. Give a 95% confidence interval for the proportion of secretaries earning less than \$25,000 a year.

Exercise 7

Find the minimum sample size required for the overall proportion of voters who prefer Candidate Y over Candidate Z to within 2% with 90% confidence. (Assume that no guess as to what that proportion might be is available.)

Exercise 8

A television station wants to estimate the proportion of the viewing audience in its area that watch its evening news. Find the minimum sample size required to estimate that proportion to within 3% with 95% confidence if . . .

- (a) no guess as to the value of that proportion is available.
 - (b) it is known that the station's evening news reaches at most 30% of the viewing audience.
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Exercise 9

Consider the following random sample which was obtained from a normal distribution with some unknown mean μ and unknown variance σ^2 :

$$x_1 = 16, x_2 = 12, x_3 = 18, x_4 = 13, x_5 = 21, x_6 = 15, x_7 = 8, x_8 = 17$$

- (a) Construct a 95% confidence interval for σ .
 - (b) Construct a 95% confidence lower bound for σ .
 - (c) Construct a 95% confidence upper bound for σ .
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Exercise 10

In a comparative study of two new drugs, A and B, 120 patients were treated with drug A and 150 patients with drug B, and the following results were obtained.

Exercise 11

A national equal employment opportunities committee is conducting an investigation to determine if female employees are as well paid as their male counterparts in comparable jobs. Random samples of 14 males and 11 females in junior academic positions are selected, and the following calculations are obtained from their salary data.

	Male	Female
Sample Mean	\$48,530	\$47,620
Sample Standard Deviation	\$780	\$750

Assume that the populations are normally distributed with equal variances.